DATA MINING TECHNIQUES IN ELECTRICITY PRICING

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Competitive Electricity Markets

The electricity business was born in 1882 when T. Edison built the first commercial power generation and distribution system in New York City.

At first, the electric systems were local affairs providing power only for neighborhood areas.

However, these territories began to overlap, and that was the first time for the competition in electricity supply.

Infrastructure grew in scale and as consolidation in ownership occurred, the industry began to take on the characteristics of a „natural monopoly”.

Competitive Electricity Markets

The last three decades have seen radical changes in the electricity market structure around the world.

At the beginning there are widespread concern about competition and power system security are mutually exclusive.

A number of unique features in comparison with any other commodity.

- large volatility in electric prices as a consequences of the high variability in demand and large differences in the cost of electricity production.

- Electricity cannot be stored transmission congestion can lead to a temporary geographical fragmentation of the market
Competitive Electricity Markets

The electricity business, competitive or otherwise, comprises five more or less mutually exclusive services

- generation: production of wholesale quantities of power;
- transmission: the transportation of wholesale power over large distance using high voltage cable networks;
- Ancillary services: products to balance supply and demand in real time and maintain overall system security;
- distribution: the transportation of power from the transmission system to the consumer;
- wholesale/retail supply: services to facilitate the purchase and sale of the physical commodity (marketing/supply, metering, billing);
Customer characterization

The market liberalization has been given a greater degree of freedom in fixing tariff rates, respecting a set of regulatory rules.

Detailed knowledge of the customer behavior is thus essential for designing specific tariff options supplying the various types of customers.

Customer characterization: adequate information on the consumption patterns of customers.

Load profiling: tools used to perform customer characterization forming customer classes based on consumer load curves.

Load classification: models which assign different consumers to existing classes.
The main objectives of the presentation

1. Comparisons of several data mining techniques for consumer load characterization
   - classical multivariate statistical methods
     * SPSS 15.0 for Windows
       (SPSS Inc., Chicago, USA)
   - computational intelligence approaches
     * NeuralWorks Predict
       (NeuralWare Inc., Pittsburg, USA)

2. Application of load characterization for procurement cost calculations
Data mining techniques for consumer load characterization

Consumer load profiling

- cluster analysis
- self-organizing maps

Consumer load classification

- discriminant analysis
- three-layer feed forward neural networks
Measurement data

All metered historical data for consumers of E.ON Energy Service.
Quarter hourly data from January to December in the years of 2005, 2006, 2007.
After data compression and filtering we have hourly normalized weekly load curves for 1231 consumers.
(representative weekly loads)
Representative weekly load curves

**Historical data**

**Typical weekly loads for each month of the year**

**Representative weekly load curve**

Typical weekly load:
Average value of the quarter hourly loads for each day of the week (Monday, Tuesday,…,Saturday)

Normalized weekly load:
Typical weekly load was normalized by the average weekly load on hourly basis

Representative weekly load:
Average value of the monthly normalized weekly loads
Consumer Load Profiling

Let \( w_j^2 = \frac{1}{|C_j|} \sum_{r_i \in C_j} |r_i - c_j|^2 \) be the average of mean square distance between weekly loads in \( j \)-th group and group center \( c_j \), where \( |C_j| \) denotes the number of patterns in \( j \)-th group. (\( j = 1, 2, \ldots, M \)).

Mean Index Adequacy (MIA)

\[ MIA = \sqrt{\frac{1}{M} \sum_{j=1}^{M} w_j^2} \]
Consumer Load Profiling

Classical multivariate statistical methods
- K-mean \((\text{MacQeen})\)
- hierarchical

Computational intelligence approaches
- self-organizing map \((\text{Kohonen})\)

<table>
<thead>
<tr>
<th>Method</th>
<th>Adequacy Indices</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>MSE</td>
</tr>
<tr>
<td>K-Mean</td>
<td>5.579</td>
</tr>
<tr>
<td>Hierarchical</td>
<td>5.938</td>
</tr>
<tr>
<td>SOM</td>
<td>3.890</td>
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</tbody>
</table>
Consumer Classification

Classical multivariate statistical method
- discriminant analysis
  - linear, quadratic.

Computational intelligence approach
- Three-layer feed-forward neural networks

<table>
<thead>
<tr>
<th>Method</th>
<th>Correct classification (%)</th>
<th>Neural network</th>
<th>Learning set</th>
<th>Average</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Average</td>
<td>Max</td>
<td>Min</td>
<td></td>
</tr>
<tr>
<td>Linear</td>
<td>90.8</td>
<td>97.0</td>
<td>80.5</td>
<td></td>
</tr>
<tr>
<td>Quadratic</td>
<td>94.7</td>
<td>100.0</td>
<td>87.5</td>
<td></td>
</tr>
<tr>
<td>Neural Network</td>
<td>96.0</td>
<td>100.0</td>
<td>93.4</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Learning set</th>
<th>Correct classification (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1231 (100%)</td>
<td>96.0</td>
</tr>
<tr>
<td>925 (75%)</td>
<td>94.2</td>
</tr>
<tr>
<td>615 (50%)</td>
<td>91.3</td>
</tr>
</tbody>
</table>
Consumer Load Profiling

Consumer group 2

Typical Weekly Load
Lower bound
Upper bound

Hours (kW/kW)

0 1 2 4 6 8 10 12 14 16 18 20

Hours

0 24 48 72 96 120 144 168

(kW/kW)
Consumer Load Profiling

Consumer group 12

Typical Weekly Load

Lower bound

Upper bound

(kW/kW)

Hours

0 12 24 36 48 60 72 84 96 108 120 132 144 156 168

(kW/kW)

Hours

0 12 24 36 48 60 72 84 96 108 120 132 144 156 168
Aggregated electric loads for the consumer group 12

Yearly load pattern

Weekly load pattern

MONTHLY LOADS

Average
Maximum
Minimum

Days
0 25 50 75 100 125 150 175 200 225 250 275 300 325 350
MW

0 25 50 75 100 125 150 175 200 225 250 275 300 325 350
MW

0
2
4
6
8
10
12

0
96
192
288
384
480
576
672

Quarter hours

MW

0
1 2 3 4 5 6 7 8 9 10 11 12

Months

MW

Max
Min

0 96 192 288 384 480 576 672

Quarter hours

MW

0 96 192 288 384 480 576 672

Quarter hours

MW

0 96 192 288 384 480 576 672

Quarter hours
Consumer Load Profiling

Clustering results in the plain of the first two canonical variables
**Consumer Load Profiling and procurement costs**

**European Energy Exchange (EEX)**

Block products considering average of the hourly EEX spot prices over the time interval of blocks:

<table>
<thead>
<tr>
<th>No.</th>
<th>PRODUCTS</th>
<th>Time period</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Base-load</td>
<td>00-24</td>
</tr>
<tr>
<td>2</td>
<td>Weekdays  Peak</td>
<td>08-20</td>
</tr>
<tr>
<td>3</td>
<td>Holidays  Peak</td>
<td>08-20</td>
</tr>
<tr>
<td>4</td>
<td>Weekdays  Base-load</td>
<td>00-24</td>
</tr>
<tr>
<td>5</td>
<td>Holidays  Base-load</td>
<td>00-24</td>
</tr>
<tr>
<td>6</td>
<td>Weekdays  Off-peak</td>
<td>21-07</td>
</tr>
<tr>
<td>7</td>
<td>Holidays  Off-peak</td>
<td>21-07</td>
</tr>
<tr>
<td>8</td>
<td>Weekdays  Peak</td>
<td>06-22</td>
</tr>
<tr>
<td>9</td>
<td>Holidays  Peak</td>
<td>06-22</td>
</tr>
<tr>
<td>10</td>
<td>Weekdays  Morning</td>
<td>07-11</td>
</tr>
<tr>
<td>11</td>
<td>Weekdays  High Noon</td>
<td>12-14</td>
</tr>
<tr>
<td>12</td>
<td>Weekdays  Afternoon</td>
<td>15-18</td>
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Consumer Load Profiling and procurement costs

The task is to cover the consumer load of a given consumer group using block products and balancing energy at minimum procurement cost.

**Objective function** *(non-linear and non-convex)*: 
(Block capacity x Time interval) x Product price.

**Independent variable** *(continuous or integer)*: 
Block capacity.

**Constraints** *(linear)*: 
• for the products (capacity and time interval) 
• lower and upper bound for under and over covering.

*Premium Solver Platform 8.0*  
(Frontline Systems, Inc. Inline Village, NV, USA)
Consumer Load Profiling and procurement costs

Result of the optimized purchase costs using 12 products
Consumer Load Profiling and procurement costs

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<th>Proc. Cost</th>
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<td>0.500</td>
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<tr>
<td>8</td>
<td>5.655</td>
<td>1.393</td>
</tr>
<tr>
<td>14</td>
<td>13.241</td>
<td>1.876</td>
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**Volatility index**

Euclidean distance between the normalized load curve and the constant load with value 1.0.
Consumer Load Profiling and procurement costs

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Procurement costs versus volatility index
Electricity Pricing based on consumer classification

Data compression and normalization

Electric loads in 2nd week of February
(Shopping Center)

Typical Weekly Load
Lower bound
Upper bound
Shopping Center

Volatility Index
Relative Procurement Cost

Volatility Index
Relative Procurement Cost

Consumer classification

Consumer GROUP 2
Conclusions

Consumer load profiling

• Computational intelligence methods performed better in comparison with classical multivariate approaches

Consumer load classification

• Three-layer feed-forward neural network performed the best classification accuracy

Consumer load characterization and procurement cost

• There is a relatively simple relationship between the procurement cost and volatility index